

Stat Support Activity: Correlation Coefficient Analysis

Notes:

- When two different quantitative variables with different units are related or associated, we say there is correlation between the variables.
- The Correlation Coefficient (r) is a number between -1 and $+1$ that determines the strength and direction of the correlation.
- If the Correlation Coefficient (r) is close to zero on the number line, then the two quantitative variables have not correlation.
- If the Correlation Coefficient (r) is close to $+1$ on the number line, then the two quantitative variables have a strong positive correlation.
- A positive correlation also indicates that the two quantitative variables are directly related. As one variable (x) increases, the other variable (y) also tends to increase. The scatterplot of the data will have a spread pattern that generally goes up from left to right.
- If the Correlation Coefficient (r) is close to -1 on the number line, then the two quantitative variables have a strong negative correlation.
- A negative correlation also indicates that the two quantitative variables are inversely related. As one variable (x) increases, the other variable (y) decreases. As one variable (x) decreases, the other variable (y) increases. The scatterplot of the data will have a spread pattern that generally goes down from left to right.
- Coefficient of Determination (r^2): This number is calculated by squaring the Correlation Coefficient (r) and will also need to be converted to a percentage. It is the proportion or percentage of variability in the response variable (y) that can be explained by the linear relationship with the explanatory variable (x). Note: The Correlation Coefficient (r) is NOT a proportion so should NEVER be converted to a percentage.
- If r is close to $+1$ (like $r = +0.893$) then there is a Strong, Positive Correlation (line going up from left to right (positive slope) and the points in scatterplot are close to line) ,
($r \approx +0.6, +0.7, +0.8, +0.9$ usually indicate pretty strong positive correlation)
- If r is close to -1 (like $r = -0.916$) then there is a Strong Negative Correlation (line going down from left to right (negative slope) and the points in the scatterplot are close to the line)
($r \approx -0.6, -0.7, -0.8, -0.9$ usually indicate pretty strong negative correlation)
- If r close to zero (like $+0.037$ or -0.009) then there is a No linear correlation. Points in the scatterplot do not follow any linear pattern. There still could be a nonlinear curved pattern though. ($r \approx \pm 0.1, \pm 0.0$ usually indicate no linear correlation)
- If $r \approx \pm 0.2, \pm 0.3$ usually indicate very weak linear correlation. There is some linear pattern but the points are very far from the regression line.

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- If $r \approx \pm 0.4, \pm 0.5$ usually indicate moderate linear correlation. There is a linear pattern and points are only moderately close to the regression line.

Directions: Fill out the following table.

	Correlation Coefficient (r)	Coefficient of Determination Proportion (r^2)	Coefficient of Determination Percentage (r^2)	Strength of the Correlation (<u>Strong</u> , <u>Moderate</u> , <u>Weak</u> , or <u>No Correlation</u>)	If there is some correlation, what is the direction of correlation? (<u>Positive</u> or <u>Negative</u>)	If there is some correlation, are the two quantitative variables <u>directly</u> related or <u>inversely</u> related?
1.	+0.273					
2.	-0.875					
3.	0					
4.	+0.581					
5.	-0.118					
6.	+0.924					
7.	-0.512					
8.	+0.041					
9.	-0.236					
10.	+0.701					
11.	-0.933					