## Stat Support Activity: Regression Lines

## Notes

- Regression Line ("Line of Best Fit" or "Line of Least Squares") is the line that best fits ordered pair quantitative data.
- Regression Line Equation: $\widehat{y}=b_{0}+\left(b_{1} \times x\right)$ where $b_{1}$ is the slope and $b_{0}$ is the y-intercept. Note: Replace $b_{1}$ and $b_{0}$ with numbers but leave the $\widehat{y}$ and the $x$ in the equation.
- Slope ( $b_{1}$ ) is the amount of increase or decrease in the response variable (y) per unit of $x$.
- Slope Equation: $b_{1}=\frac{\left(r \times s_{y}\right)}{s_{x}}$ where $r$ is the correlation coefficient, $s_{x}$ is the standard deviation of the explanatory ( $x$ ) column of data, and $s_{y}$ is the standard deviation of the response ( $y$ ) column of data.
- Y-intercept Equation: $b_{0}=\bar{y}-\left(b_{1} \times \bar{x}\right)$ where $b_{1}$ is the slope, $\bar{x}$ is the mean average of the explanatory ( $x$ ) column of data, and $\bar{y}$ is the mean average of the response ( y ) column of data.

Directions: Fill out the following table to calculate the slope and y-intercept for the regression line and then write the regression line equation. Round the slope and y-intercept to the thousandths place ( 3 numbers to the right of the decimal).

|  | Correlation Coefficient (r) | Standard <br> Deviation <br> of $x$ <br> column <br> ( $\boldsymbol{s}_{x}$ ) | Standard <br> Deviation <br> of $y$ <br> column <br> ( $\boldsymbol{s}_{\boldsymbol{y}}$ ) | Slope $\begin{aligned} & \left(b_{1}\right)= \\ & \frac{\left(r \times s_{y}\right)}{s_{x}} \end{aligned}$ | Mean of $\boldsymbol{x}$ column $(\bar{x})$ | Mean of $y$ column $(\overline{\boldsymbol{y}})$ | $\begin{gathered} \text { Y-intercept } \\ \left(b_{0}\right)= \\ \bar{y}-\left(b_{1} \times \bar{x}\right) \end{gathered}$ | Regression Line Equation $\widehat{y}=b_{0}+\left(b_{1} \times x\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | 0.961 | 0.313 | 4.632 |  | 0.941 | 12.103 |  |  |
| 2. | -0.575 | 1.288 | 0.341 |  | 6.591 | 0.527 |  |  |
| 3. | 0.991 | 43.844 | 10.209 |  | 133.0 | 68.357 |  |  |
| 4. | -0.358 | 0.099 | 0.054 |  | 0.763 | 0.453 |  |  |
| 5. | 0.348 | 2.290 | 2.607 |  | 6.778 | 6.333 |  |  |
| 6. | -0.711 | 2.182 | 17.433 |  | 13.4 | 255.6 |  |  |
| 7. | 0.751 | 69.897 | 155.297 |  | 77.404 | 280.912 |  |  |
| 8. | -0.649 | 4.116 | 1.792 |  | 21.725 | 10.388 |  |  |

