

Stat Support Activity: Two-Population Proportion Z-test statistic Calculations (Updated Version)

1.

We want to compare the population percentage of people that identify as men and have at least one tattoo (π_1) and the population percentage of people that identify as women and have at least one tattoo (π_2). A random sample of 857 people that identify as men found that 146 of them had at least one tattoo. A random sample of 794 people that identify as women found that 137 of them had at least one tattoo. Calculate the Z-test statistic to compare the sample proportions.

- a) Calculate sample proportion 1 (\hat{p}_1) for men with a tattoo.

$$\hat{p}_1 = \frac{x_1}{n_1} = \frac{\text{amount in sample 1}}{\text{total sample 1}}$$

- b) Calculate sample proportion 2 (\hat{p}_2) for women with a tattoo.

$$\hat{p}_2 = \frac{x_2}{n_2} = \frac{\text{amount in sample 2}}{\text{total sample 2}}$$

- c) Calculate the sample proportion difference $\hat{p}_1 - \hat{p}_2$ by subtracting the answers in part (a) and part (b).

- d) Calculate p-pooled (\bar{p}) = $\frac{(x_1 + x_2)}{(n_1 + n_2)}$ =

- e) Calculate the complement of p-pooled ($1 - \bar{p}$) by subtracting your answer in letter (d) from 1.

- f) The standard error has been calculated for you using p-pooled, 1 minus p-pooled, and the formula.

$$\text{Standard Error} = \sqrt{\left(\frac{\bar{p}(1-\bar{p})}{n_1} + \frac{\bar{p}(1-\bar{p})}{n_2}\right)} = 0.01856$$

- g) Calculate the two-population Z-test statistic by dividing the answers to part (c) and part (f).

$$\text{Z - test statistic} = \frac{\text{sample proportion difference}}{\text{standard error}} = \frac{(\hat{p}_1 - \hat{p}_2)}{\text{standard error}} =$$

- h) Z – test statistic sentence: The sample proportion for men with at least one tattoo was _____ standard errors (*above or below*) the sample proportion for women with at least one tattoo. (Note: Use “above” if Z – test stat is positive. Use “below” if Z – test stat is negative.)

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2.

A random sample of 135 women that smoke (population 1) found that 38 were able to get pregnant in the allotted amount of time. A random sample of 543 women that do not smoke (population 2) found that 206 were able to get pregnant in the allotted amount of time.

- a) Calculate sample proportion 1 (\hat{p}_1) of smoking women that were able to get pregnant.

$$\hat{p}_1 = \frac{x_1}{n_1} = \frac{\text{amount in sample 1}}{\text{total sample 1}}$$

- b) Calculate sample proportion 2 (\hat{p}_2) of non-smoking women that were able to get pregnant.

$$\hat{p}_2 = \frac{x_2}{n_2} = \frac{\text{amount in sample 2}}{\text{total sample 2}}$$

- c) Calculate the sample proportion difference $\hat{p}_1 - \hat{p}_2$ by subtracting the answers in part (a) and part (b).

- d) Calculate p-pooled (\bar{p}) = $\frac{(x_1 + x_2)}{(n_1 + n_2)}$ =

- e) Calculate the complement of p-pooled ($1 - \bar{p}$) by subtracting your answer in letter (d) from 1.

- f) The standard error has been calculated for you using p-pooled, 1 minus p-pooled, and the formula.

$$\text{Standard Error} = \sqrt{\left(\frac{\bar{p}(1-\bar{p})}{n_1} + \frac{\bar{p}(1-\bar{p})}{n_2}\right)} = 0.04616$$

- g) Calculate the two-population Z-test statistic by dividing the answers to part (c) and part (f).

$$Z - \text{test statistic} = \frac{\text{sample proportion difference}}{\text{standard error}} = \frac{(\hat{p}_1 - \hat{p}_2)}{\text{standard error}} =$$

- h) Z – test statistic sentence: The sample proportion of smoking women that were able to get pregnant was _____ standard errors (*above or below*) the sample proportion of non-smoking women that were able to get pregnant. (Note: Use “above” if Z – test stat is positive. Use “below” if Z – test stat is negative.)

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3. Sample 1: People that do NOT use Marijuana but do use other drugs.
Sample 2: People that use Marijuana and other drugs.

	Use Other Drugs	Total
Sample 1 (Do not use Marijuana)	26	219
Sample 2 (Use Marijuana)	87	213

- a) Calculate sample proportion 1 (\hat{p}_1) of non-marijuana users that use other drugs.

$$\hat{p}_1 = \frac{x_1}{n_1} = \frac{\text{amount in sample 1}}{\text{total sample 1}}$$

- b) Calculate sample proportion 2 (\hat{p}_2) of marijuana users that use other drugs.

$$\hat{p}_2 = \frac{x_2}{n_2} = \frac{\text{amount in sample 2}}{\text{total sample 2}}$$

- c) Calculate the sample proportion difference $\hat{p}_1 - \hat{p}_2$ by subtracting the answers in part (a) and part (b).

- d) Calculate p-pooled (\bar{p}) = $\frac{(x_1 + x_2)}{(n_1 + n_2)}$

- e) Calculate the complement of p-pooled ($1 - \bar{p}$) by subtracting your answer in letter (d) from 1.

- f) The standard error has been calculated for you using p-pooled, 1 minus p-pooled, and the formula.

$$\text{Standard Error} = \sqrt{\left(\frac{\bar{p}(1-\bar{p})}{n_1} + \frac{\bar{p}(1-\bar{p})}{n_2}\right)} = 0.0423$$

- g) Calculate the two-population Z-test statistic by dividing the answers to part (c) and part (f).

$$Z - \text{test statistic} = \frac{\text{sample proportion difference}}{\text{standard error}} = \frac{(\hat{p}_1 - \hat{p}_2)}{\text{standard error}} =$$

- h) Z – test statistic sentence: The sample proportion of non-marijuana users that use other drugs was _____ standard errors (*above or below*) the sample proportion of marijuana users that use other drugs. (*Note: Use “above” if Z – test stat is positive. Use “below” if Z – test stat is negative.*)